

# **Performance Modeling Strategies for Modern Reinforced Concrete Bridge Columns**

**Michael P. Berry  
Marc O. Eberhard  
University of Washington**

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# UW-PEER Structural Performance Database

- Nearly 500 Columns
  - spiral or circular hoop-reinforced columns (~180)
  - rectangular reinforced columns (~300)
- Column geometry, material properties, reinforcing details, loading
- Digital Force-Displacement Histories
- Observations of column damage
- <http://nisee.berkeley.edu/spd>
- User's Manual (Berry and Eberhard, 2004)



# Objective of Research

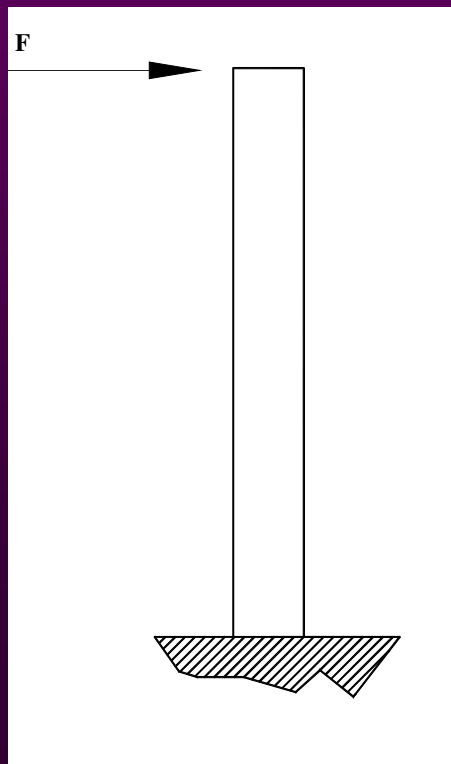
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**Develop, calibrate, and evaluate column modeling strategies that are capable of accurately modeling bridge column behavior under seismic loading.**

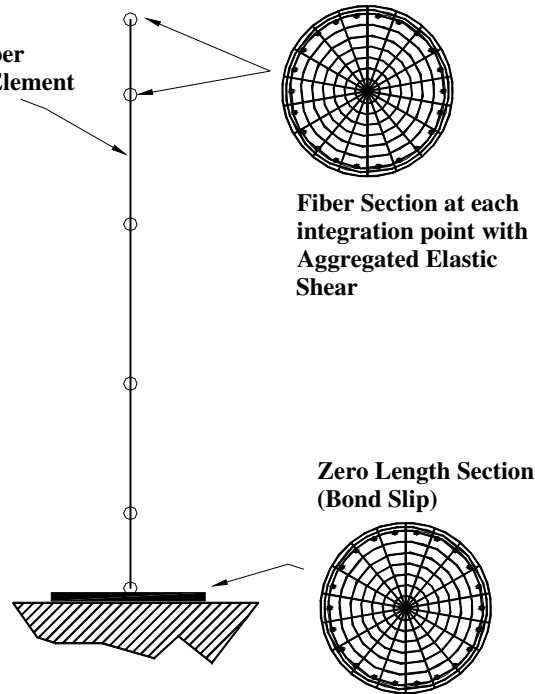
- Global deformations**
- Local deformations (strains and rotations)**
- Progression of damage**

# Advanced Modeling Strategies

## Distributed-Plasticity



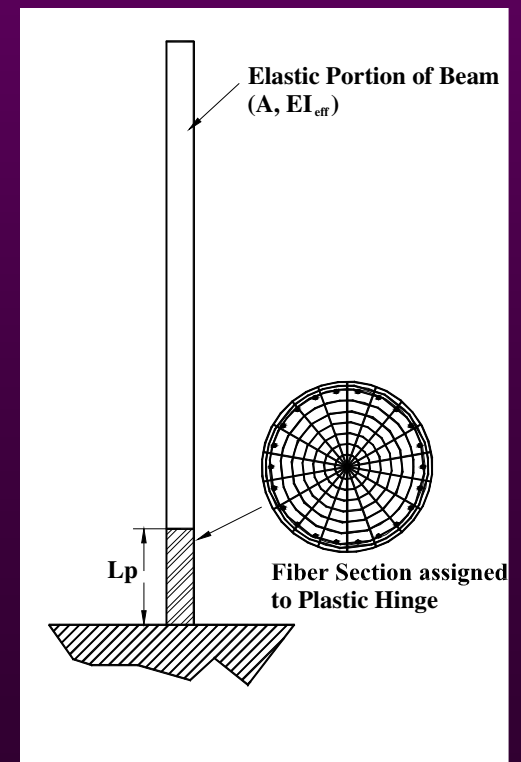
Force-Based Fiber  
Beam Column Element  
(Flexure)



Fiber Section at each  
integration point with  
Aggregated Elastic  
Shear

Zero Length Section  
(Bond Slip)

## Lumped-Plasticity



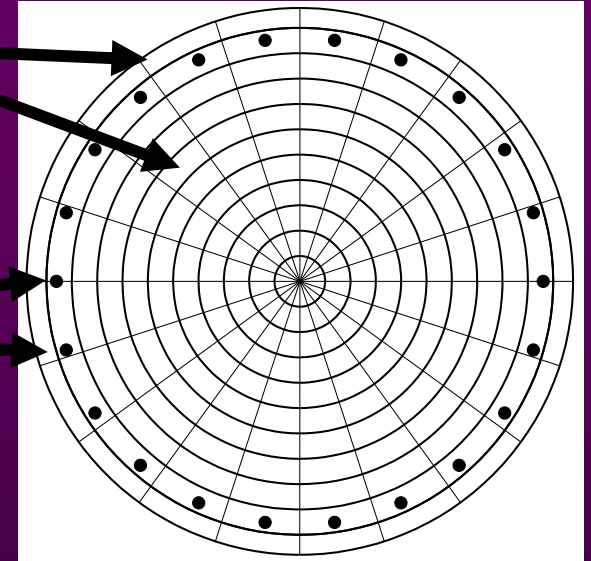
# Cross-Section Modeling

# Cross-Section Modeling Components

- Concrete Material Model

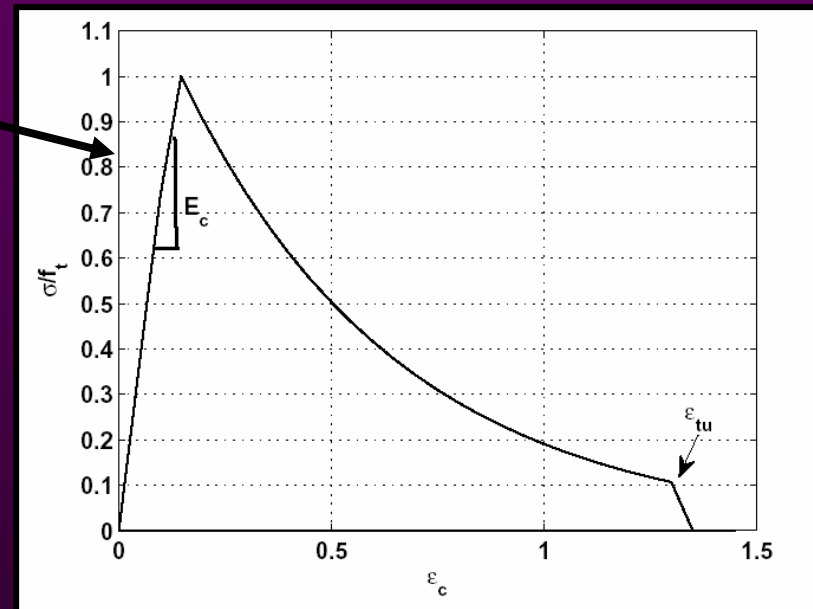
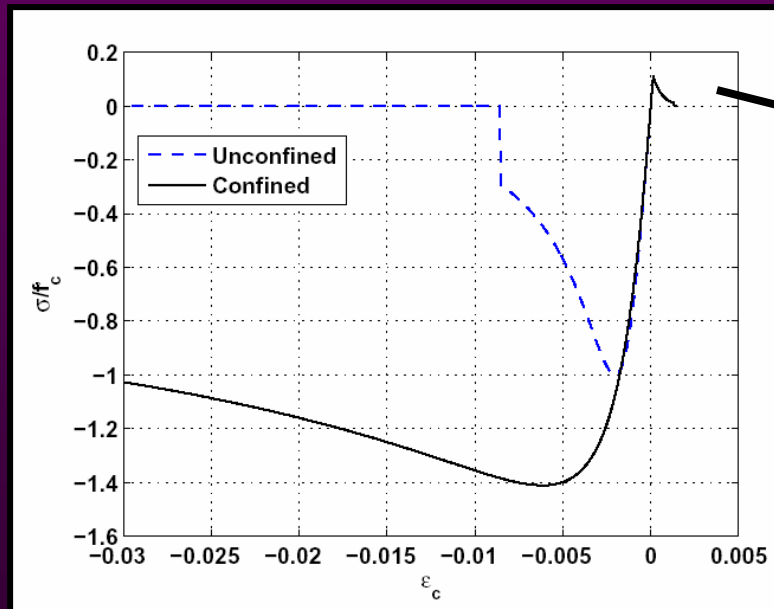
- Reinforcing Steel Material Model

- Cross-Section Discretization Strategy

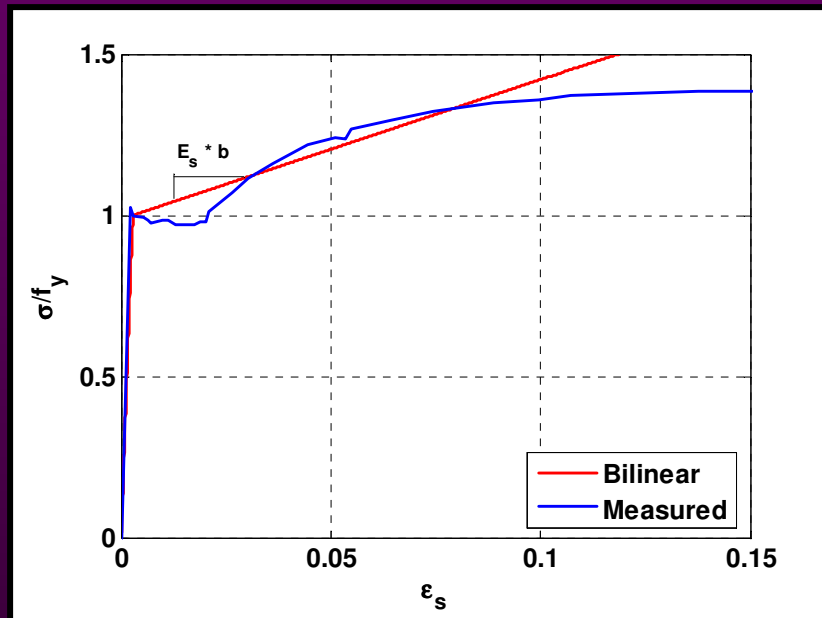


# Concrete Material Model

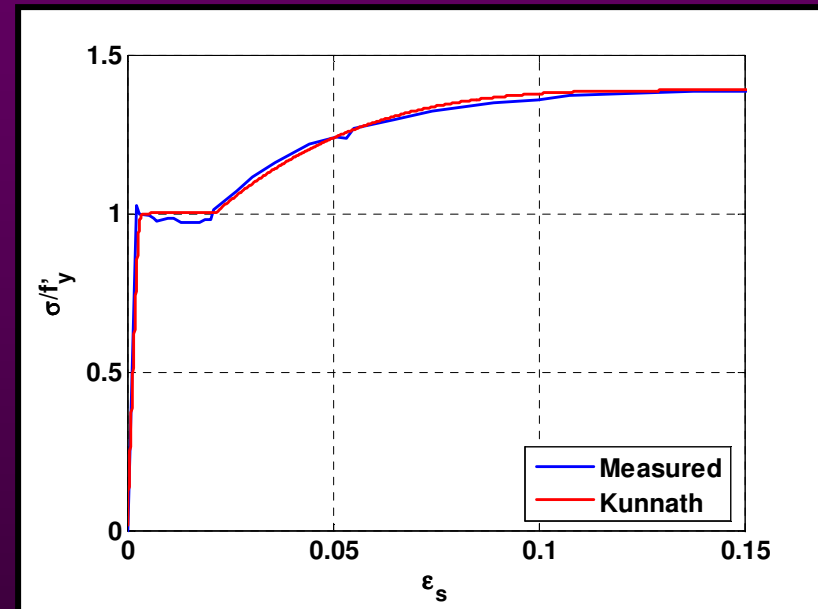
Popovic's Curve with Mander et. al. Constants and  
Added Tension Component (Concrete04)



# Reinforcing Steel Material Models



Giufre-Menegotto-Pinto  
(Steel02)

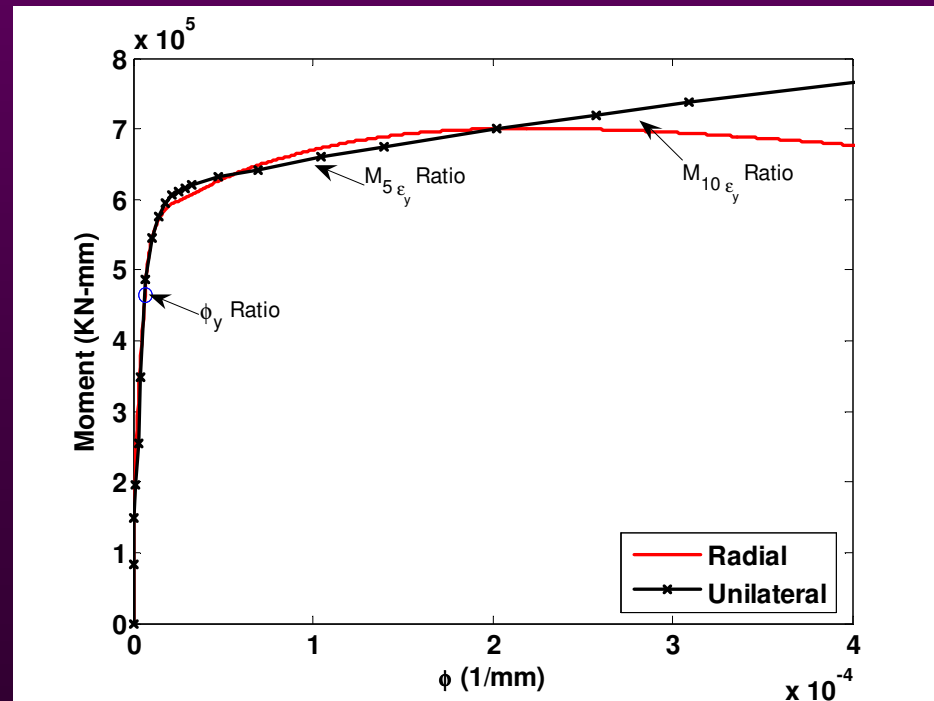
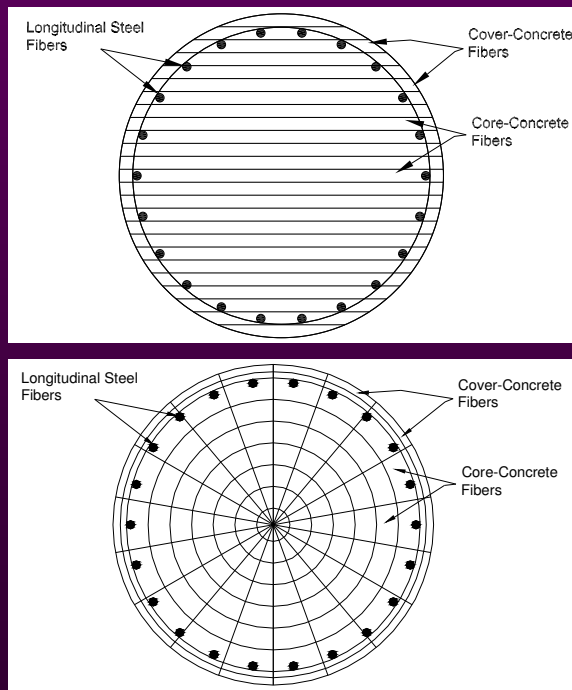


Mohle and Kunnath  
(ReinforcingSteel)



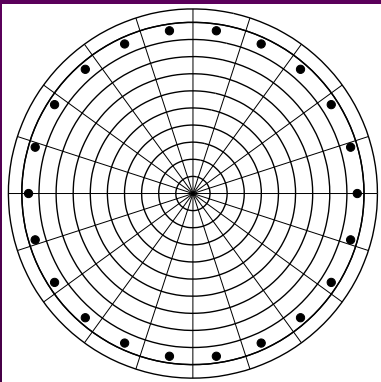
# Section Fiber Discretization

- **Objective:** Use as few fibers as possible to eliminate the effects of discretization



# Cross-Section Fiber Discretization

## Uniform (220 Fibers)



### Confined

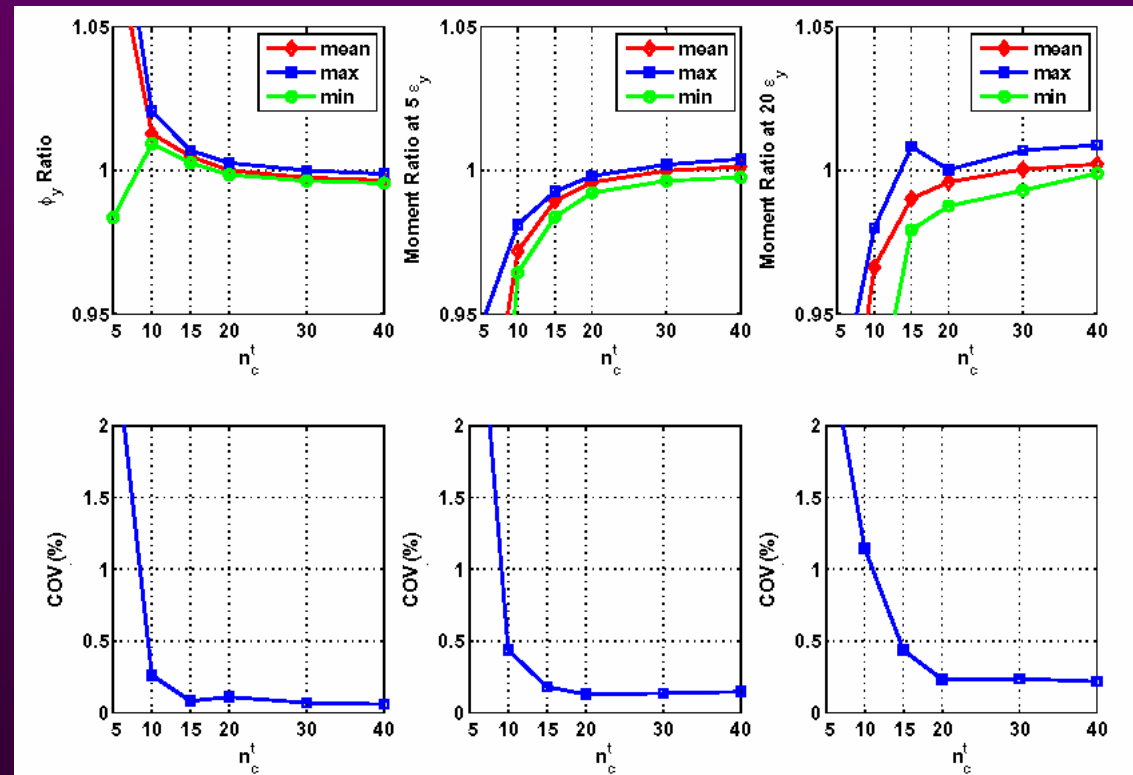
$$n_c^r = 10$$

$$n_c^t = 20$$

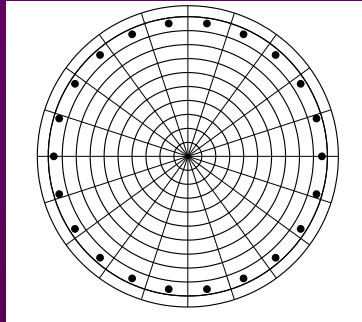
### Unconfined

$$n_u^r = 1$$

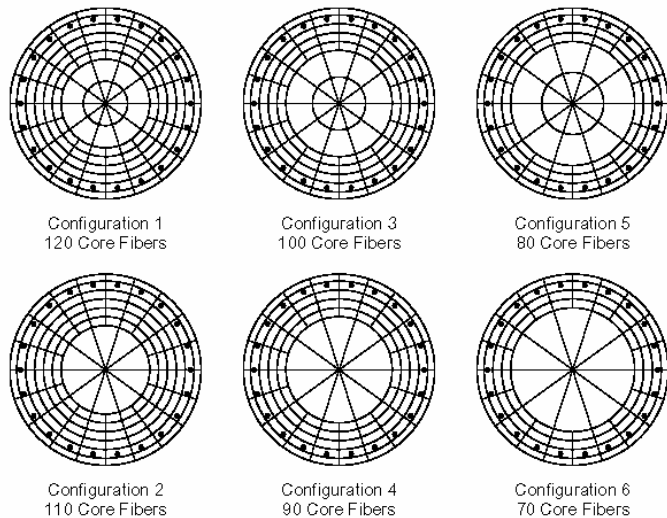
$$n_u^t = 20$$



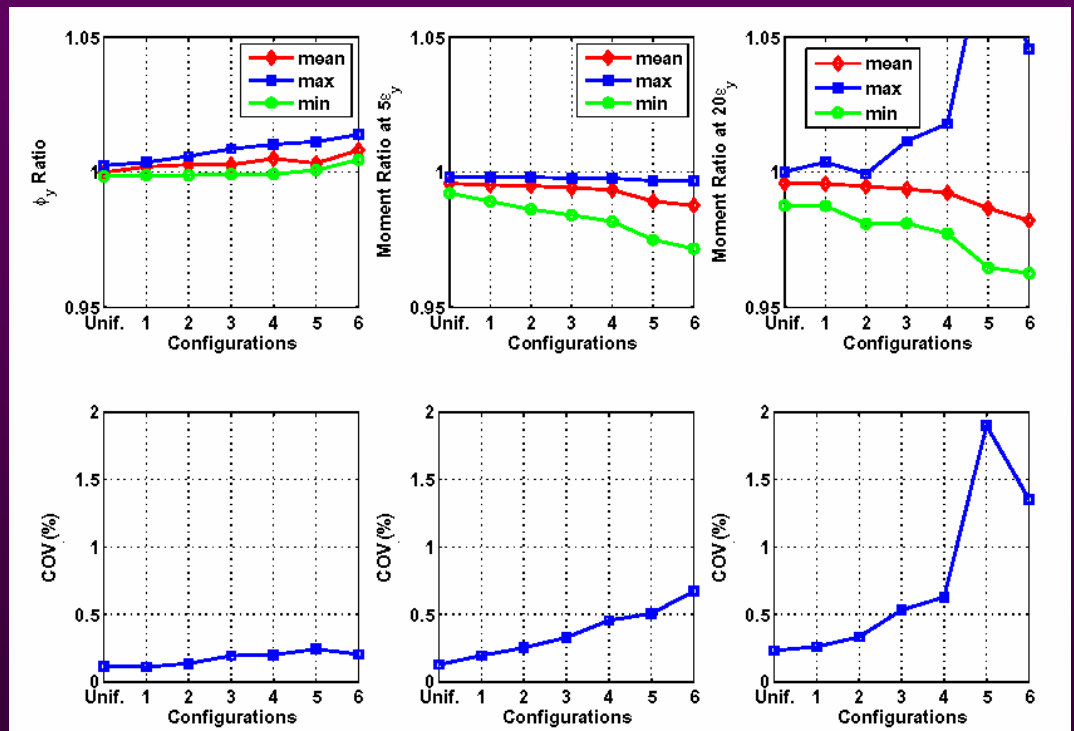
# Reduced Fiber Discretization



Uniform (220 Fibers)

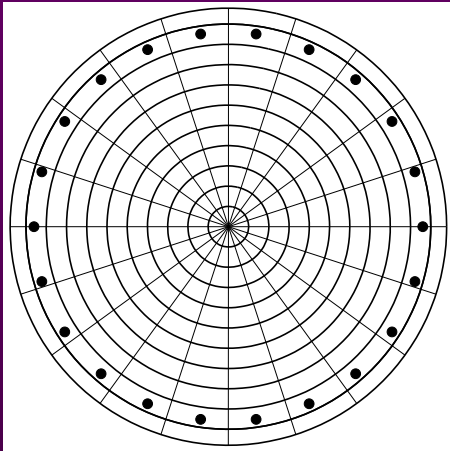


Nonuniform Strategies

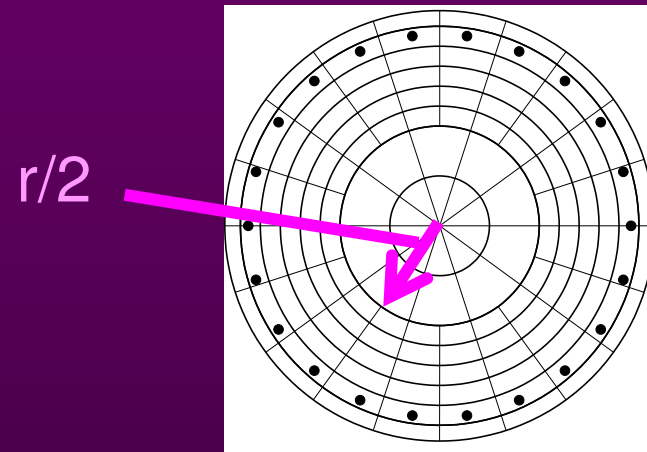


# Cross-Section Fiber Discretization

**Uniform (220 Fibers)**



**Reduced (140 Fibers)**



**Confined**

$$n_c^r = 10$$

$$n_c^t = 20$$

**Unconfined**

$$n_u^r = 1$$

$$n_u^t = 20$$

**Confined**

$$n_{fine}^r = 5$$

$$n_{fine}^t = 20$$

$$n_{coarse}^r = 2$$

$$n_{coarse}^t = 10$$

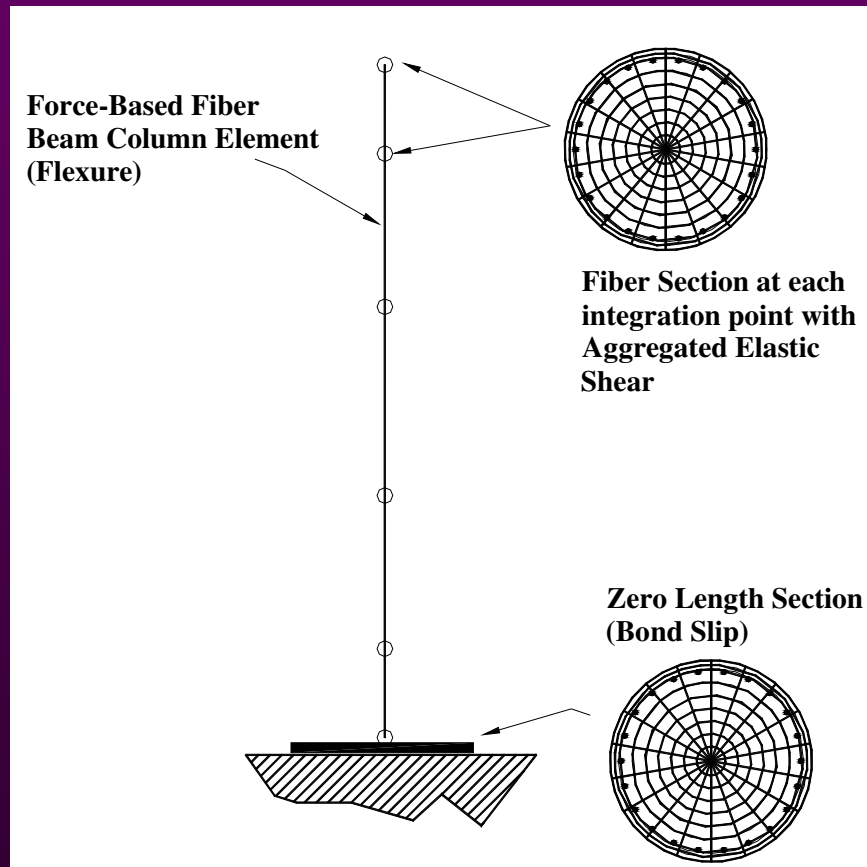
**Unconfined**

$$n_u^r = 1$$

$$n_u^t = 20$$

# **Modeling with Distributed- Plasticity Element**

# Model Components

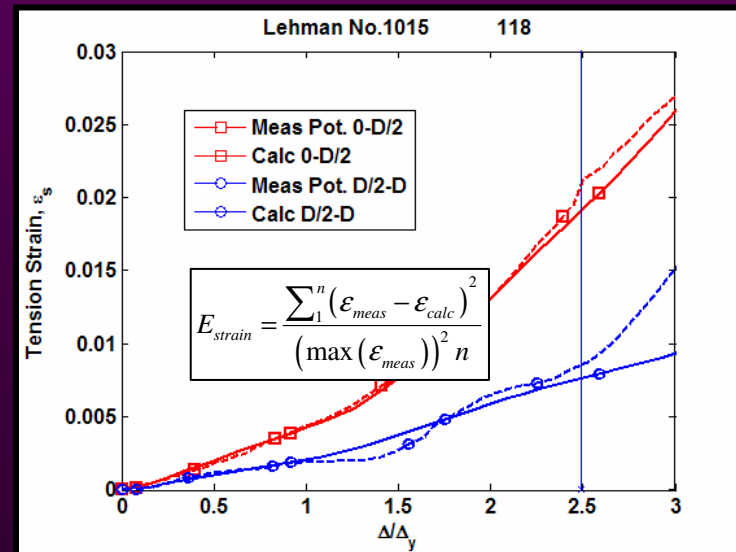
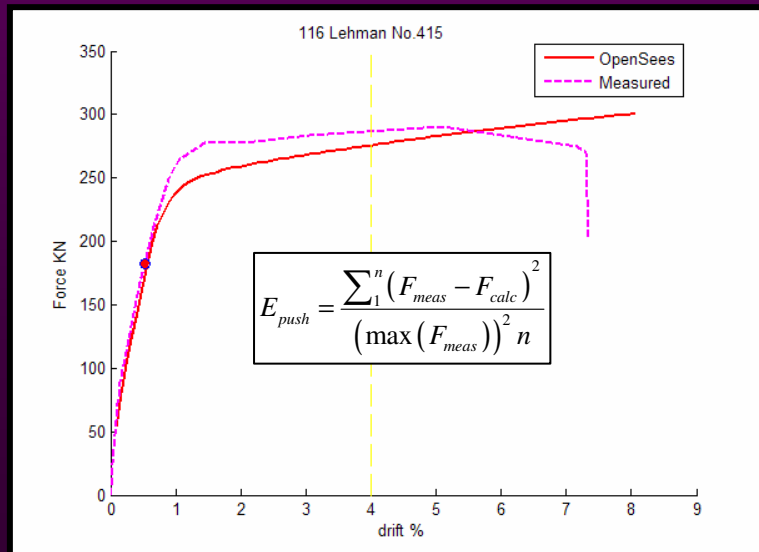


- **Flexure Model (Force-Based Beam-Column)**
  - *nonlinearBeamColumn*
  - Fiber section
  - Popovics Curve (Mander constants)
  - Giufre-Menegotto-Pinto (***b***)
  - Number of Integration Points ( $Np$ )
- **Anchorage-Slip Model**
  - *zeroLengthSection*
  - Fiber section
  - Reinforcement tensile stress-deformation response from Lehman et. al. (1998) bond model ( $\lambda$ )
  - Effective depth in compression ( $d_{comp}$ )
- **Shear Model**
  - *section Aggregator*
  - Elastic Shear ( $\gamma$ )

# Model Optimization

- **Objective:** Determine model parameters such that the error between measured and calculated global and local responses are minimized.

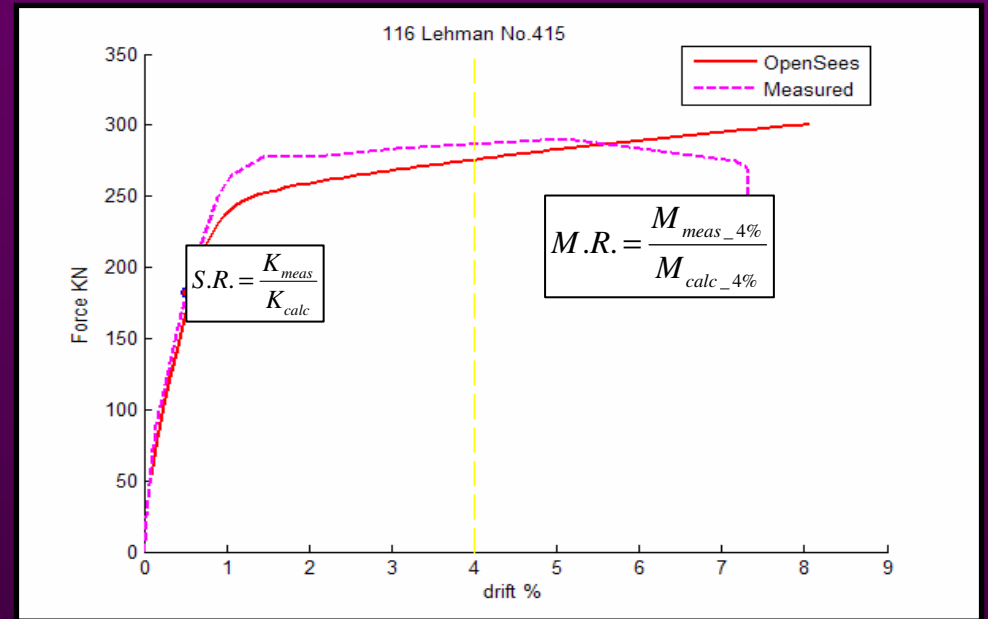
$$E_{total} = \text{mean}(E_{push}) + \frac{\kappa_1}{2} \text{mean}(E_{strain}^{(0-D/2)}) + \frac{\alpha_2}{2} \text{mean}(E_{strain}^{(D/2-D)})$$



# Model Evaluation

## Optimized Model:

- Strain Hardening Ratio,  $b = 0.01$
- Number of Integration Points,  $N_p = 5$
- Bond-Strength Ratio,  $\lambda = 0.875$
- Bond-Compression Depth,
- $d_{comp} = 1/2$  N.A. Depth at 0.002 comp strain
- Shear Stiffness  $\gamma = 0.4$

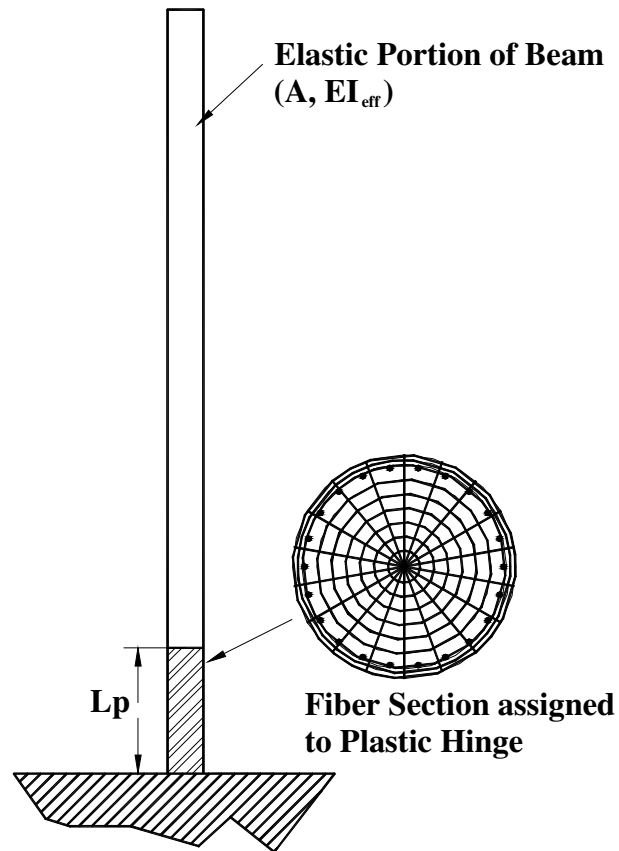


	$E_{total}$	$E_{push}$	$E_{strain}^{(0-D/2)}$	$E_{strain}^{(D/2-D)}$	$S.R.$	$M.R.$
mean	14.89	6.73	7.78	14.4	1.02	1.03
cov (%)	—	—	—	—	15	8



# **Modeling with Lumped- Plasticity Element**

# Lumped-Plasticity Model



- Hinge Model Formulation:
  - *beamwithHinges3*
  - Force Based Beam Column Element with Integration Scheme Proposed by Scott and Fenves, 2006.
  - Fiber Section
- Elastic Section Properties
  - Elastic Area,  $A$
  - Effective Section Stiffness,  $EI_{eff}$
- Calculated Plastic-Hinge Length
  - $L_p$

# Section Stiffness Calibration

	Stiffness Ratio Stats	
$EI_{eff} =$	$\alpha_g^{calc} E_c I_g$	$\alpha_{sec}^{calc} EI_{sec}$
mean	1.00	1.00
cov (%)	19	16

$$\alpha_g^{calc} = 0.1 + 0.034 \frac{L}{D} + 1.35 \frac{P}{A_g f'_c} \leq 1.0$$

$$\alpha_{sec}^{calc} = 0.45 + 0.087 \frac{L}{D} \leq 1.0$$

# Plastic-Hinge Length Calibration

$$L_p = 0.05L + 0.1 \frac{f_y d_b}{\sqrt{f'_c}} \leq \frac{L}{4}$$

$$\epsilon_{bb}^{calc} = 0.046 + 0.25\rho_{eff} \leq 0.15$$

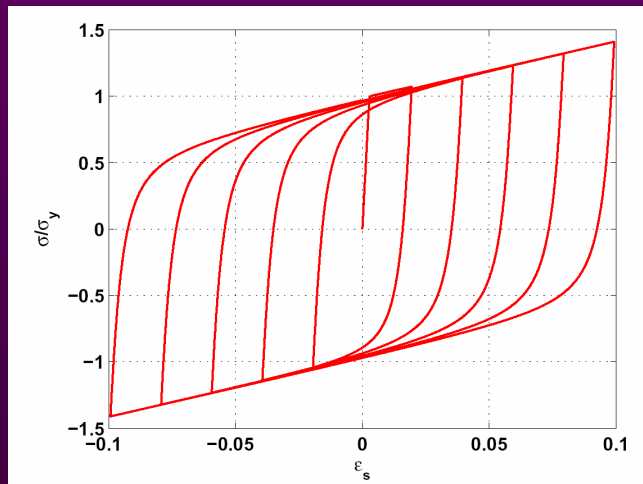
		Pushover Accuracy			Damage Estimates					
Plastic-Hinge Length	$E_{total}$ mean	$E_{push}$ mean	M.R. mean	D.R. mean	$\epsilon_{bb}$		$\frac{\Delta_{bb}^{meas}}{\Delta_{bb}^{calc}}$ cov	$\epsilon_{sp}$		$\frac{\Delta_{sp}^{meas}}{\Delta_{sp}^{mean}}$ cov
Selected Optimal $0.05L + 0.1 \frac{f_y d_b}{\sqrt{f'_c}} \leq L/4$	8.32	8.08	1.05	-1.23	0.082	0.299	0.237	0.008	0.482	0.350
Priestley et al. (1996) $0.08L + 0.022f_y d_b \leq 0.044f_y d_b$	8.87	8.32	1.06	-1.49	0.070	0.349	0.281	0.007	0.465	0.359
Mattock (1967) $0.05L + 0.5D$	8.96	8.41	1.07	-1.56	0.058	0.323	0.291	0.006	0.424	0.353

# **Cyclic Response**

# Cyclic Material Response

- Cyclic response of the fiber-column model depends on the cyclic response of the material models.

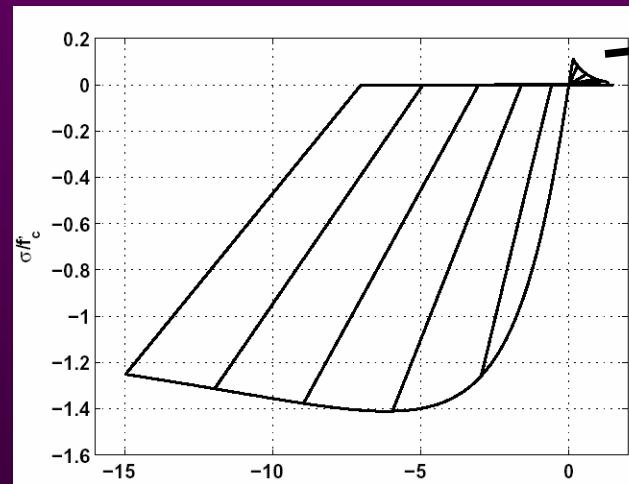
Reinforcing Steel



Giufre-Menegotto-Pinto (with Bauschinger Effect)

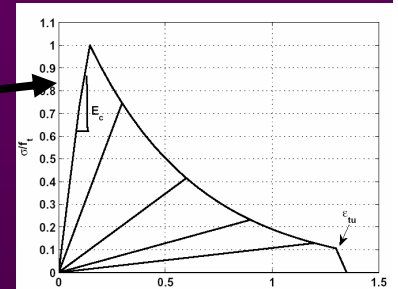
Steel02

Confined and Unconfined Concrete



Karsan and Jirsa with Added Tension Component

Concrete04

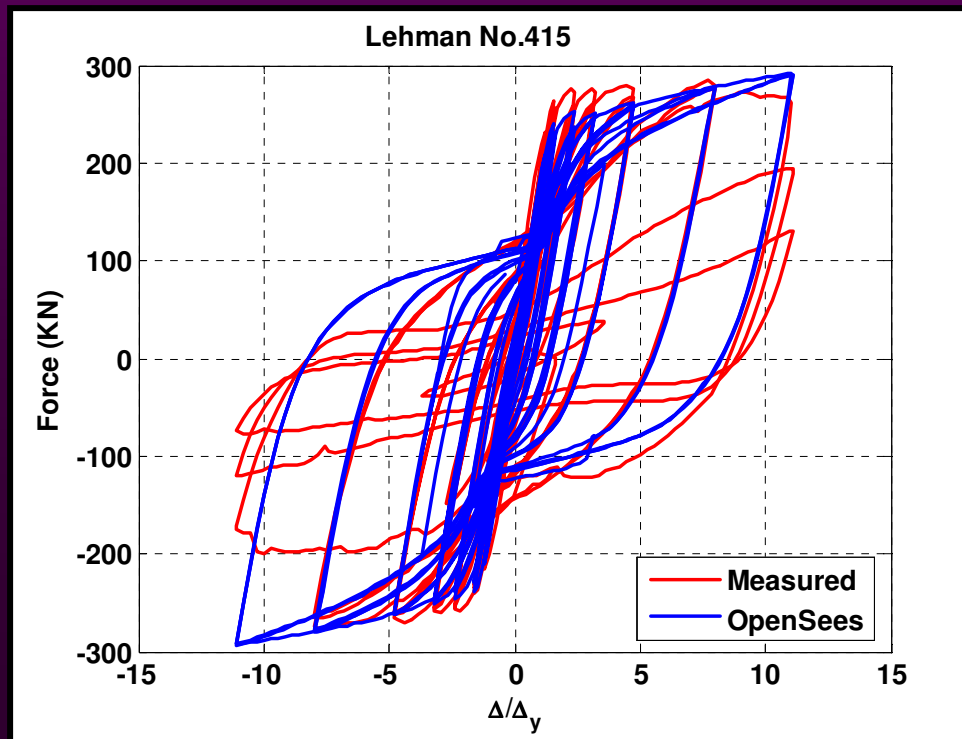


- Current Methodologies**

- Do not account for cyclic degradation steel
- Do not account for imperfect crack closure

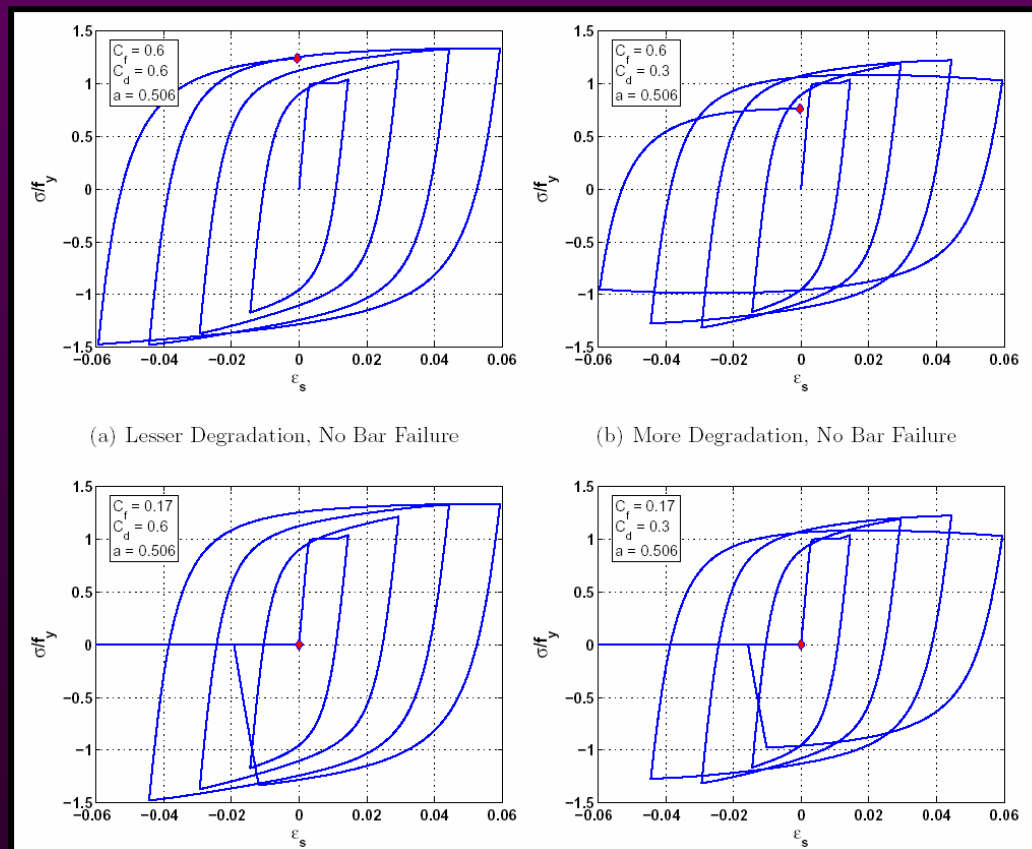
# Evaluation of Response

	Lumped-Plasticity	Distributed-Plasticity
	$E_{\text{force}} (\%)$	$E_{\text{force}} (\%)$
mean	16.13	15.66
min	6.63	6.47
max	44.71	46.05



# Kunnath and Mohle Steel Material Model

- Cyclic degradation according to Coffin and Manson Fatigue.
- Model parameters:
  - Ductility Constant,  $C_f$
  - Strength Reduction Constant,  $C_d$

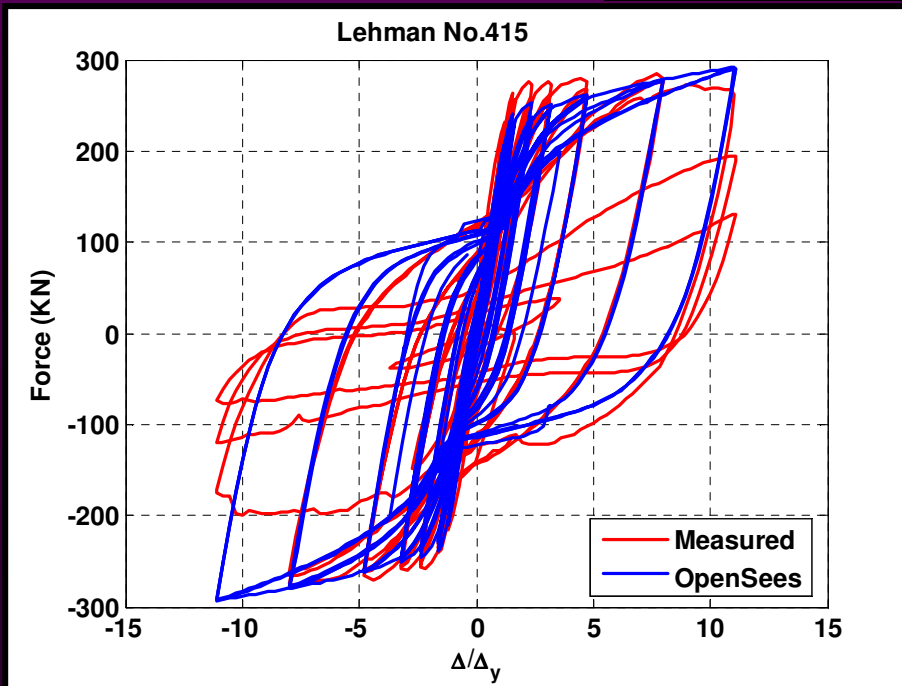




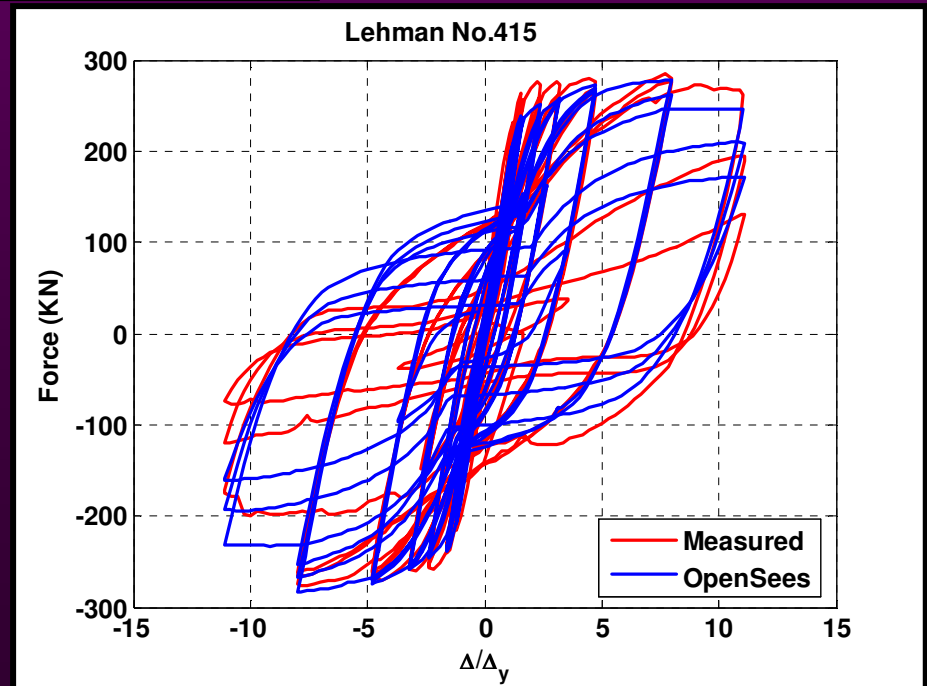
# Preliminary Study with Kunnath Steel Model

- Ductility Constant,  $C_f=0.4$
- Strength Reduction Constant,  $C_d=0.4$

	Giufre-Menegotto-Pinto	Kunnath and Mohle
	$E_{force} (\%)$	$E_{force} (\%)$
mean	16.13	11.98
min	6.63	5.15
max	44.71	29.45



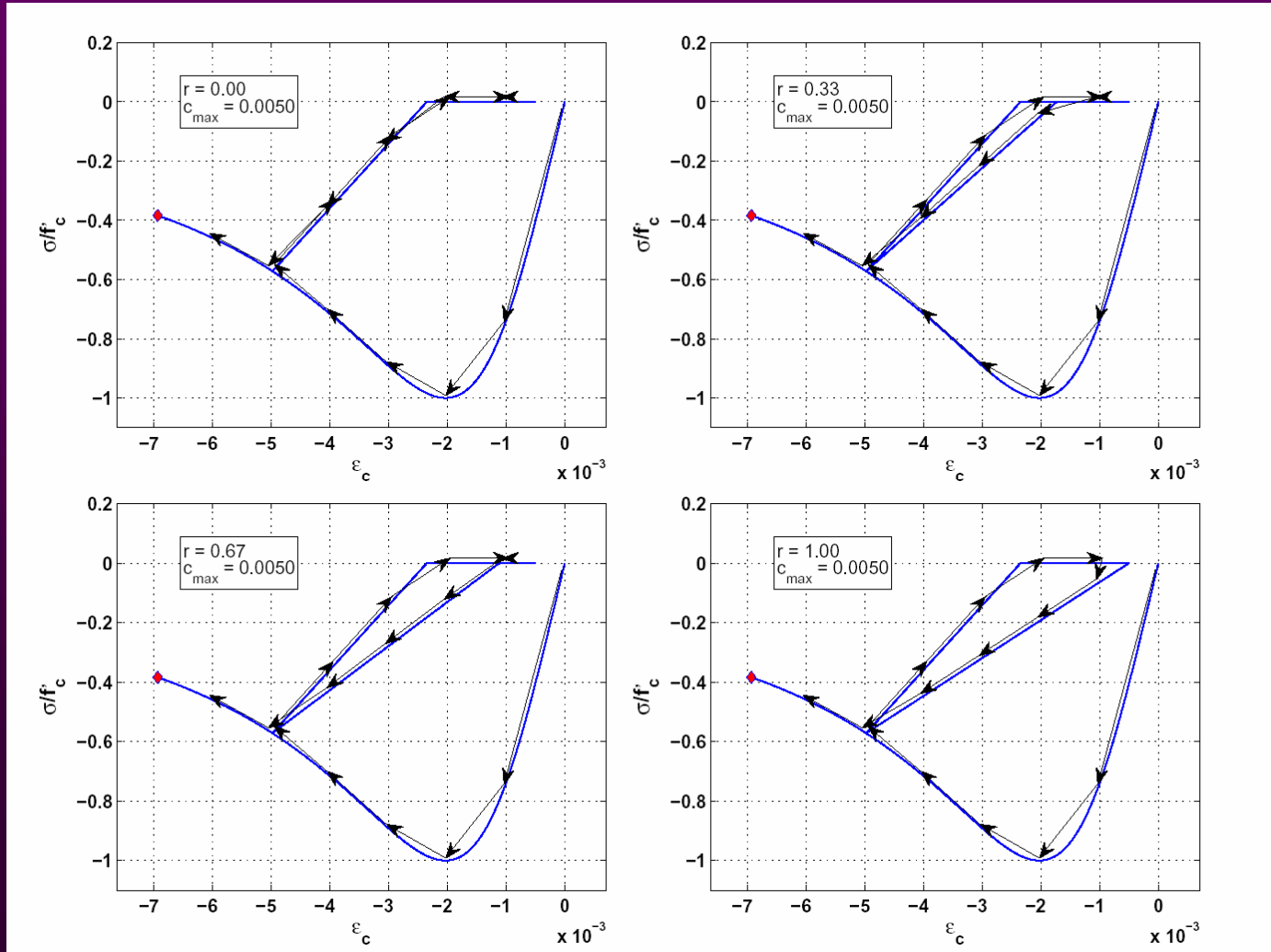
Giufre-Menegotto-Pinto (with Bauschinger Effect)



Kunnath and Mohle (2006)

# Continuing Work

# Imperfect Crack Closure



# Prediction of Flexural Damage

- Drift Ratio Equations
- Distributed-Plasticity Modeling Strategy
- Lumped-Plasticity Modeling Strategy

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graph TD; A[• Drift Ratio Equations  
• Distributed-Plasticity Modeling Strategy  
• Lumped-Plasticity Modeling Strategy] --> B[Key Statistics]; A --> C[Fragility Curves]; A --> D[Design Recommendations];
```

Key Statistics

Fragility Curves

Design  
Recommendations

# Evaluation of Modeling-Strategies for Complex Loading

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- **Bridge Bent (Purdue, 2006)**
- **Unidirectional and Bi-directional Shake Table (Hachem, 2003)**

**Thank you**